



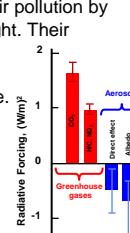
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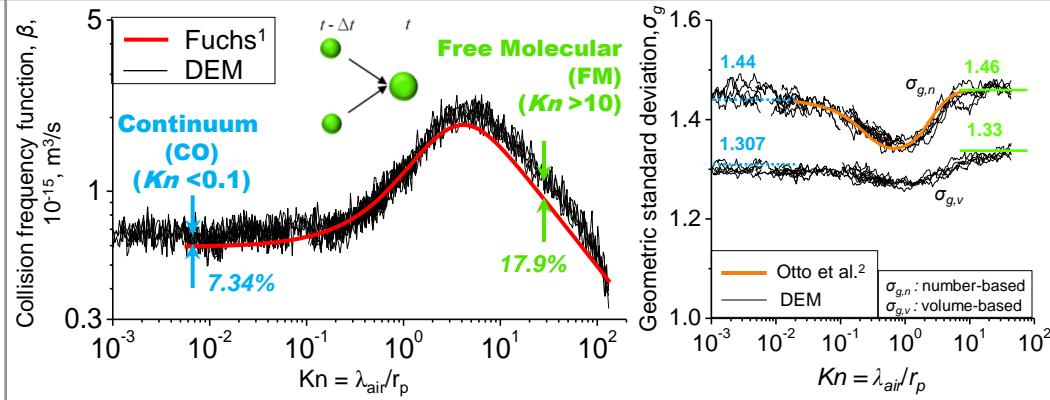
## Motivation

Brownian coagulation of fractal-like agglomerates is investigated by discrete element modeling (DEM) and population balance equations (PBE) in transition regime. Aerosols affect air pollution by absorbing & scattering light. Their structure affects handling & processing and finally agglomerate performance.

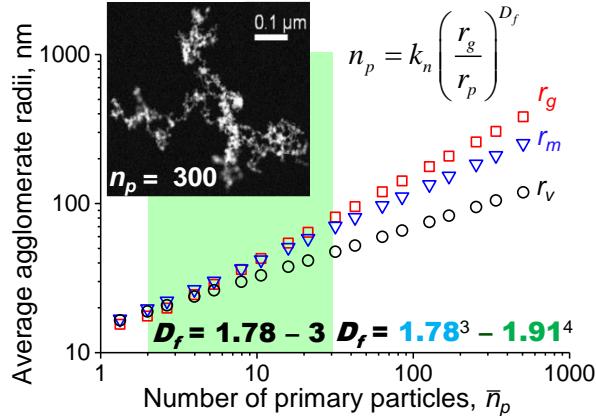
Understanding agglomerate dynamics can facilitate optimal process design of aerosols synthesis of materials, flocculation of suspensions, monitoring combustion emissions and climate modeling.



## Validation – Full Coalescence

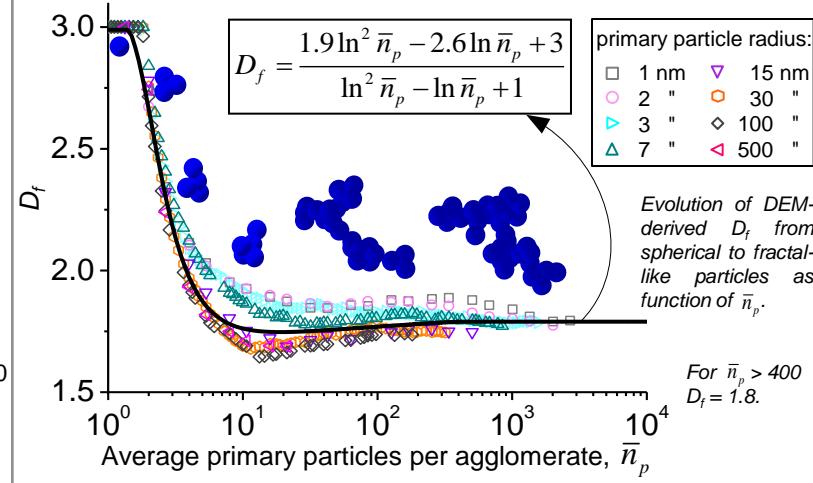


## Agglomerate Dynamics

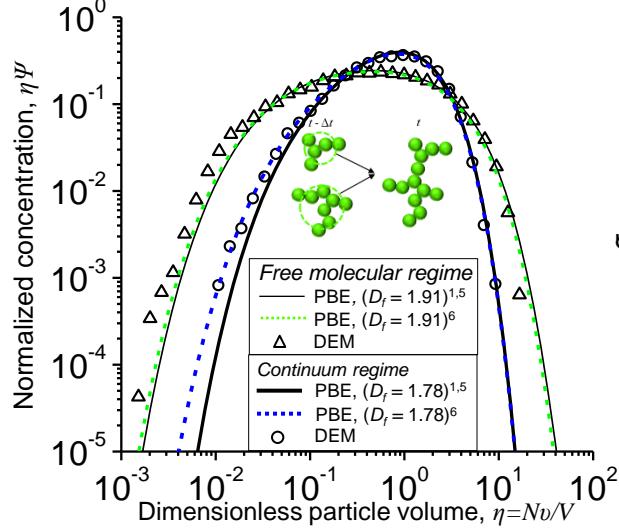


Evolution of the geometric mean gyration,  $r_g$ , mobility,  $r_m$ , and volume-equivalent,  $r_v$ , radii as a function of the number of primary particles per agglomerate,  $\bar{n}_p$ .

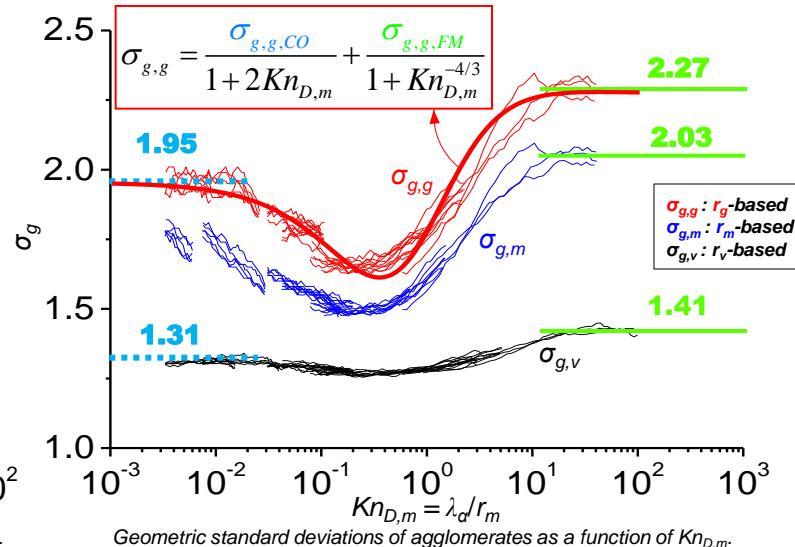
## Evolution of Fractal Dimension, $D_f$



## Self-Preserving Size Distribution (SPSD) & Geometric Standard Deviation, $\sigma_g$



SPSD of coagulating agglomerates by DEM (symbols) and PBE (lines).



Geometric standard deviations of agglomerates as a function of  $Kn_{D,m}$ .

## References

- [1] Fuchs NA. (1964) The mechanics of aerosols
- [2] Otto E, et al. (1994) Part Part Syst Charact. **11**, 359
- [3] Jullien R, Kolb M, Botet R. (1984) J. Physique. **45**, 395
- [4] Ball RC, Jullien R. (1984) J. Phys. Lett. **45**, L1031
- [5] Mountain RD, et al. (1986) J. Colloid Interface Sci. **114**, 67
- [6] Thajudeen T, et al. (2012) Aerosol Sci. Technol. **46**, 1174

## Conclusions

1. The  $r_g$ ,  $r_m$  and  $r_v$  of the same agglomerate can be significantly different for  $\bar{n}_p > 10 - 30$ .
2. The asymptotic  $D_f$  is attained for  $\bar{n}_p > 10 - 30$ .
3. Agglomerates obtain PSD with  $\sigma_{g,g} = 2.27$  and  $\sigma_{g,m} = 2.03$  in the free molecular and  $\sigma_{g,g} = 1.95$  in the continuum regime going through a minimum of 1.65 and 1.50, respectively, at  $Kn_{D,m} \approx 0.2$ .
4. The relations of  $D_f$  and  $\sigma_{g,g}$  can be used in detailed particle dynamics simulations coupled to fluid dynamics for industrial process design, air pollution, meteorology and climate dynamics.