



Calibration of Engine Exhaust CPCs: Measurement Uncertainty Following ISO 27891 Procedures



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TSI Master Reference Electrometer (MRE) calibrated by the National Physical Laboratory (UK)

Master Reference Electrometer (MRE)



Measures electrical charge concentration [C/cm³]

Inlet flow $q_{CAL,MRE}$ measured by NPL when $q_{calc,MRE}$ is set to 1 L/min:

$$q_{CAL,MRE} = 1.0173 \text{ L/min}$$

Relative expanded ($k=2$) uncertainty $U_r(q_{CAL,MRE}) = 1.5\%$

| d [nm] | Nominal C_N [cm⁻³] | $\frac{C_{Q,MRE}}{C_{Q,NPL}}$ | $U_r(k=2)$ [%] | $\frac{C_{Q,MRE}}{C_{Q,NPL}} \cdot q_{calc,MRE}$ | $U_r(k=2)$ [%] |
|------------------------|-------------------------|-------------------------------|-------------------|--|-------------------|
| 23 | 5000 | 1.015 | 3.0 | 0.998 | 3.35 |
| 41 | 5000 | 1.017 | 3.1 | 1.000 | 3.44 |
| | 2000 | 1.026 | 3.1 | 1.009 | 3.44 |
| | 4000 | 1.018 | 3.1 | 1.001 | 3.44 |
| 55 | 6000 | 1.015 | 3.0 | 0.998 | 3.35 |
| | 8000 | 1.011 | 3.0 | 0.994 | 3.35 |
| | 10000 | 1.012 | 3.0 | 0.995 | 3.35 |
| 69 | 5000 | 1.017 | 3.1 | 1.000 | 3.44 |
| Average Efficiency [-] | | 1.016 | 3.05 | 0.9994 | |
| CV | | 0.45 % | | | |

Flow-corrected average detection efficiency $\bar{\eta}_{MRE}$ of the MRE:

$$\bar{\eta}_{MRE} = \left[\frac{C_{Q,MRE}}{C_{Q,NPL}} \right] \cdot q_{calc,MRE} = 1.016 \cdot \frac{1 \text{ L/min}}{1.0173 \text{ L/min}} = 0.9994$$

Relative standard ($k=1$) uncertainty $u_r(\text{MRE})$ including flow correction:

$$u_r(\text{MRE}) = \sqrt{\left(\frac{U_r(\bar{\eta}_{MRE})}{2} \right)^2 + \left(\text{CV} \left(\frac{C_{Q,MRE}}{C_{Q,NPL}} \right) \right)^2 + \left(\frac{U_r(q_{CAL,MRE})}{2} \right)^2} = \sqrt{\left(\frac{3.05 \%}{2} \right)^2 + (0.45 \%)^2 + \left(\frac{1.5 \%}{2} \right)^2} = 1.76 \%$$

Engine Exhaust CPC (EECPC) calibrated by TSI against the Reference CPC (RCPC)



EECPCs are calibrated against the Reference CPC (RCPC)

$$\eta_{EECPC} = \frac{C_{N,EECPC} \cdot q_{calc,EECPC}}{C_{N,RCPC} \cdot q_{calc,RCPC}} \cdot \beta = \frac{C_{N,EECPC}}{C_{N,RCPC}} \cdot \eta_{RCPC} \cdot \frac{q_{RCPC}}{q_{EECPC}} \cdot \beta$$

Since the efficiency curve of the EECPC is already (nearly) flat at 41 nm, and since the reference instrument is a CPC, the influence of multiply charged particles can be neglected.

Example: EECPC detection efficiency at 41 nm

Determination of q_{RCPC} , q_{EECPC} and $u_r(q_{RCPC}/q_{EECPC})$ from five flow measurements over 15 minutes

| Run # | q_{RCPC} [L/min] | q_{EECPC} [L/min] | q_{RCPC}/q_{EECPC} [-] |
|---------|--------------------|---------------------|--------------------------|
| 1 | 1,015 | 0,9910 | 1,024 |
| 2 | 1,015 | 0,9896 | 1,026 |
| 3 | 1,014 | 0,9891 | 1,025 |
| 4 | 1,011 | 0,9886 | 1,023 |
| Average | 1,013 | 0,9894 | 1,024 |
| CV | | 0,10% | 0,13% |

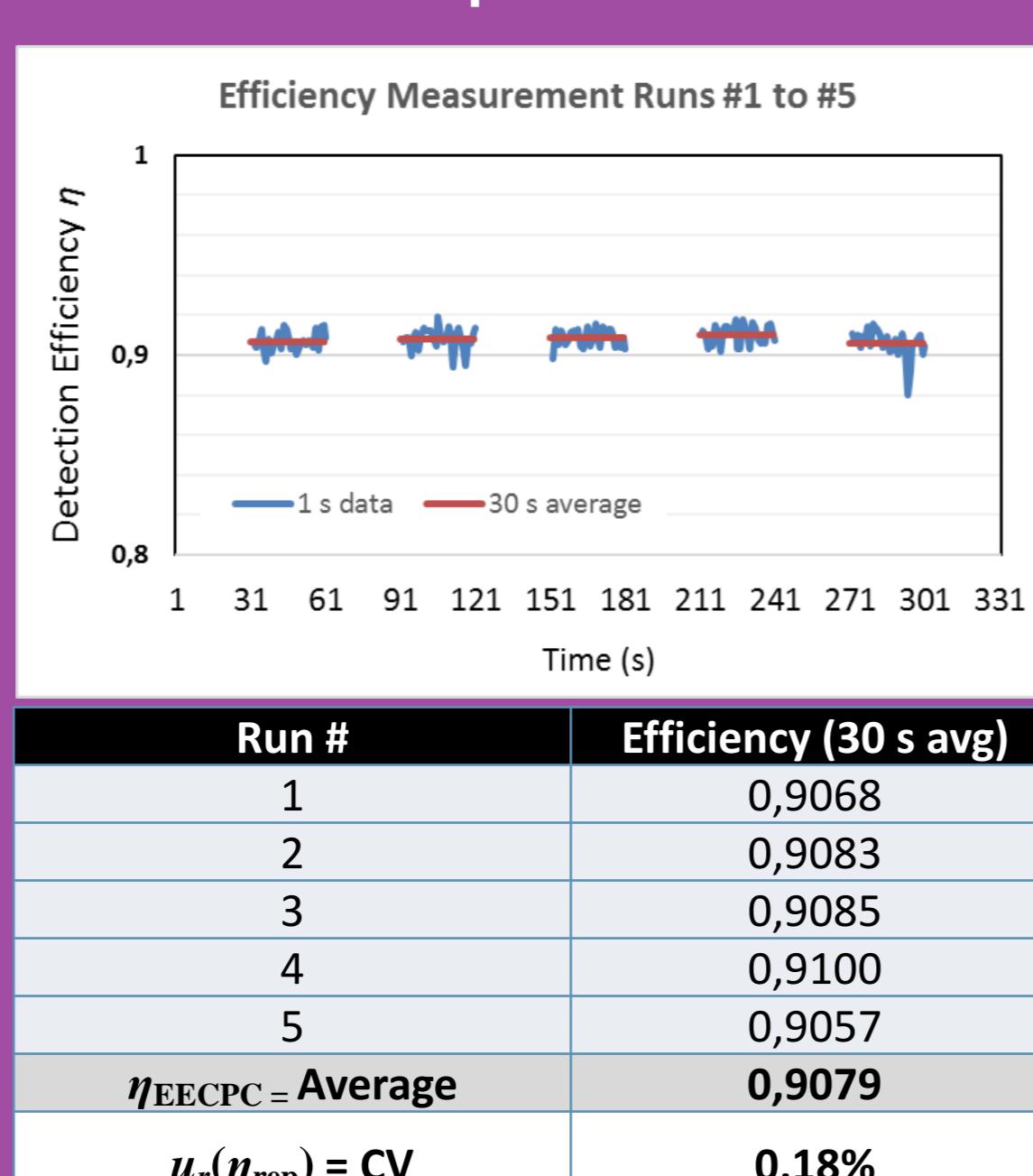
$$u_r(q_{RCPC}/q_{EECPC}) = \text{CV}(q_{RCPC}/q_{EECPC}) = 0,13 \%$$

$q_{RCPC} = 0,9894 \text{ L/min}$

$$u_r(q_{EECPC}) = \sqrt{(u_r(\text{Flowmeter}))^2 + (\text{CV}(q_{EECPC}))^2} = \sqrt{(1,23 \%)^2 + (0,10 \%)^2} = 1,23 \%$$

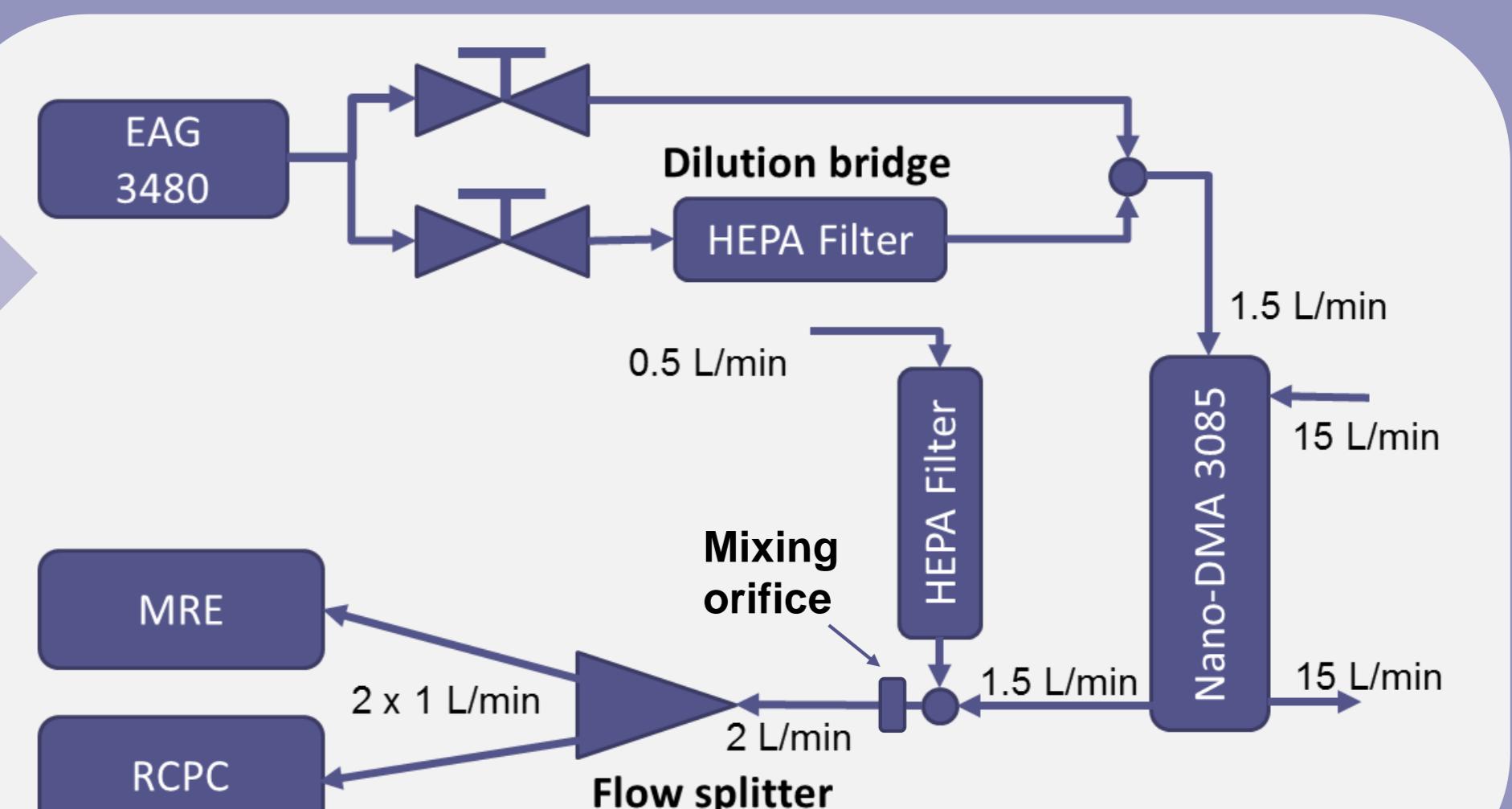
$u_r(\text{Flowmeter}) = 1,23 \%$ from the flowmeter calibration certificate

Determination of η_{EECPC} and $u_r(\eta_{rep})$ from five efficiency measurement repetitions



Reference CPC (RCPC) calibrated by TSI against the TSI Master Reference Electrometer (MRE)

The MRE is used to calibrate a Reference CPC (RCPC) at TSI



Indicated concentration of the RCPC under test
Calculated with $q_{calc,RCPC} = 1 \text{ L/min}$

Nominal RCPC inlet flow 1 L/min

Volumetric RCPC inlet flow Measured with Gillibrator®

$$\eta_{RCPC} = \frac{C_{N,RCPC} \cdot \frac{q_{calc,RCPC}}{q_{RCPC}}}{e \cdot \bar{\eta}_{MRE} \cdot q_{MRE}} \cdot \beta \cdot \sum_p \phi_p \cdot p = \text{const} \cdot \frac{C_{N,RCPC}}{I_{MRE}} \cdot \bar{\eta}_{MRE} \cdot \frac{q_{MRE}}{q_{RCPC}} \cdot \beta \cdot \sum_p \phi_p \cdot p$$

Elementary charge

Indicated, zero-corrected current of the MRE

Volumetric MRE inlet flow Measured with Gillibrator®

Contribution of multiply charged particles to I_{MRE} Measured with Tandem SMPS

Flow corrected detection efficiency of the MRE Taken from the MRE calibration certificate

Example: RCPC detection efficiency at 41 nm

Determination of q_{MRE} , q_{RCPC} and $u_r(q_{MRE}/q_{RCPC})$ from five flow measurements over 15 minutes

| Run # | q_{MRE} [L/min] | q_{RCPC} [L/min] | q_{MRE}/q_{RCPC} [-] |
|---------|-------------------|--------------------|------------------------|
| 1 | 1,021 | 1,015 | 1,0059 |
| 2 | 1,017 | 1,021 | 0,9961 |
| 3 | 1,023 | 1,017 | 1,0059 |
| 4 | 1,023 | 1,018 | 1,0049 |
| 5 | 1,024 | 1,020 | 1,0039 |
| Average | 1,022 | 1,018 | 1,0033 |
| CV | | 0,23% | 0,41% |

$$u_r(q_{MRE}/q_{RCPC}) = \text{CV}(q_{MRE}/q_{RCPC}) = 0,41 \%$$

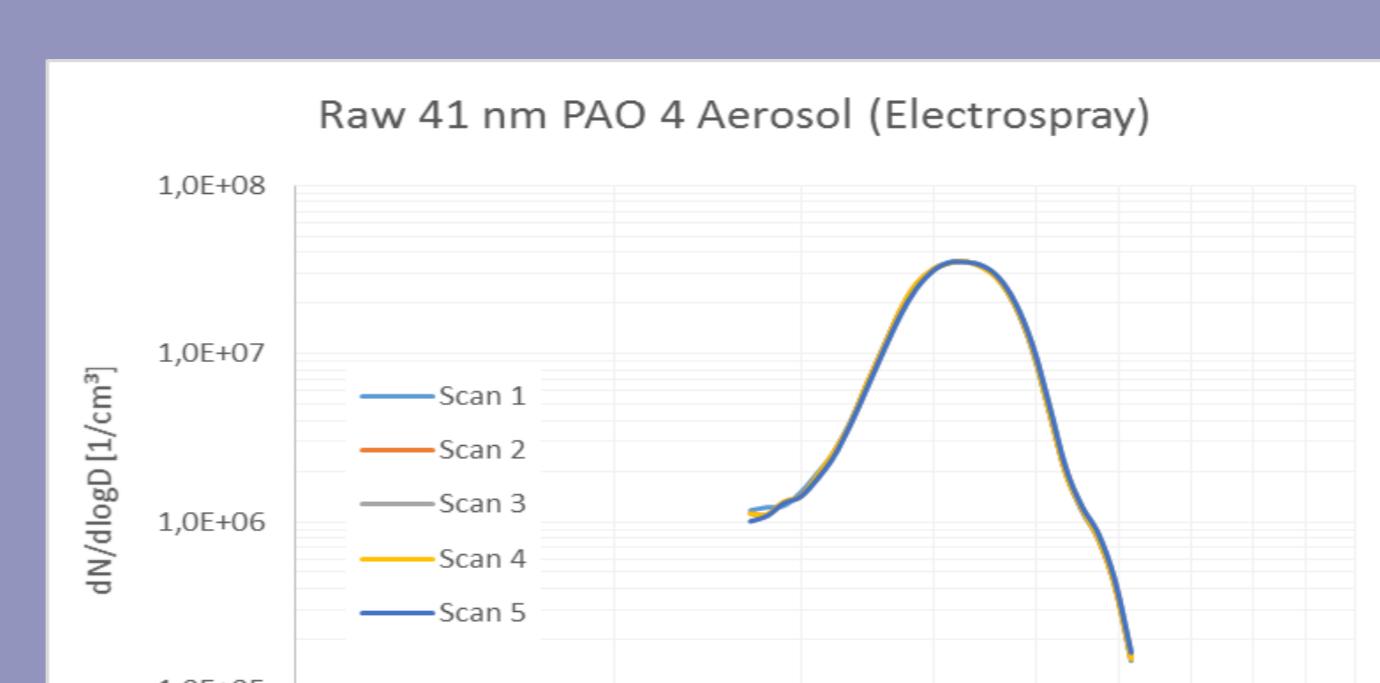
$$q_{RCPC} = 1,018 \text{ L/min}$$

$$u_r(q_{RCPC}) = \sqrt{(u_r(\text{Flowmeter}))^2 + (\text{CV}(q_{RCPC}))^2}$$

$$= \sqrt{(1,23 \%)^2 + (0,23 \%)^2} = 1,25 \%$$

$^*) u_r(\text{Flowmeter}) = 1,23 \%$ from the flowmeter calibration certificate

Determination of ϕ_p and $u_r(\sum_p \phi_p \cdot p)$ by tandem SMPS measurements (five repetitions)



| CMD [nm] | GSD [-] | N [cm⁻³] | $N(p=1)$ [cm⁻³] | $N(p=2)$ [cm⁻³] | $N(p=3)$ [cm⁻³] | $\phi_{p=1}$ | $\phi_{p=2}$ |
|---|---------|------------|-----------------|-----------------|-----------------|--------------|--------------|
| 42,1 | 1,13 | 4,31E+06 | 9,47E+03 | 1,47E+01 | --- | 9,98E-01 | 1,55E-03 |
| 42,1 | 1,13 | 4,31E+06 | 9,47E+03 | 1,46E+01 | --- | 9,98E-01 | 1,54E-03 |
| 42,2 | 1,13 | 4,29E+06 | 9,39E+03 | 1,54E+01 | --- | 9,98E-01 | 1,64E-03 |
| 42,1 | 1,13 | 4,30E+06 | 9,45E+03 | 1,46E+01 | --- | 9,98E-01 | 1,54E-03 |
| 42,2 | 1,13 | 4,30E+06 | 9,42E+03 | 1,54E+01 | --- | 9,98E-01 | 1,63E-03 |
| Average | | | | | | | |
| $u_r \left(\sum_p \phi_p \cdot p \right) = \sqrt{\frac{(\sigma(\phi_{p=1}) \cdot 1)^2 + (\sigma(\phi_{p=2}) \cdot 2)^2}{\bar{\phi}_{p=1} \cdot 1 + \bar{\phi}_{p=2} \cdot 2}} = 0,01 \%$ | | | | | | | |
| σ | | | | | | | |

Determination of η_{RCPC} and $u_r(\eta_{rep})$ from five efficiency measurement repetitions

| Run # | Efficiency (30 s avg) |
|-------|-----------------------|
| 1 | 0,9564 |
| 2 | 0,9553 |
| 3 | 0,9611 |
| 4</td | |